

**EFFICIENT NOTCH COEFFICIENT COMPUTATION FOR A DISC
DRIVE CONTROL SYSTEM USING FIXED POINT MATH**

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Field Of The Invention

The present invention relates generally to the use of notch filters in
10 digital control systems of disc drives. In particular, the present invention
provides a method and apparatus for efficiently calculating notch filter
coefficients to compensate for the resonant frequencies of a particular disc
drive.

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Background of the Invention

Modern disc drive designs use digital feedback control systems to
control the position of the head with respect to the tracks on the recording
surface of the disc. Because disc drives and their electrical control systems,
20 like all complex physical systems, are susceptible to resonance at particular
frequencies, the feedback control system that is used to control the
movement of the actuator arm generally employs one or more digital notch
filters at some point in the feedback loop. These digital notch filters must
be calibrated to attenuate the particular resonant frequencies of the
25 particular disc drive in which the filters are used. In other words, a set of
constant coefficients for each digital notch filter must be determined so that
the filter attenuates an actual resonant frequency of the disc drive.

Since the resonant frequencies of disc drive may vary from drive to
drive, it is not sufficient to find a single set of coefficients for a given
30 design. Rather, each disc drive must be individually calibrated. At present,
this calibration process generally takes place at the time of media
certification, which is when the manufacturer uses the assembled drive to

scan the recording media for defects and marks defective disc sectors as unusable. Manufacturers run a series of tests to determine the resonant frequencies of the drive. The disc drive, in turn, uses these resonant frequencies to look up filter coefficients in a table of coefficient values for various frequencies and programs its notch filters using the coefficients
5 retrieved from the table.

Table lookup, however, requires that all coefficient values be stored in memory. This makes it more complicated and costly to obtain precise filter coefficient values for a given design, since finer levels of precision
10 require more firmware memory to store more filter coefficient values. What is needed, then, is a way to achieve precise filter calibration while minimizing memory usage. The present invention provides a solution to this and other problems, and offers other advantages over previous solutions.

Summary of the Invention

The present invention provides a method and apparatus for
5 efficiently calculating notch filter coefficients for a disc drive actuator arm
control system. In a preferred embodiment, filter coefficients for a z-
domain notch-filter transfer function are calculated in fixed-point
arithmetic from polynomial interpolations of the non-linear functions that
define the coefficients in terms of the notch frequency. These non-linear
10 functions may be derived and interpolated *a priori* by applying the bilinear
transform to an s-domain notch transfer function. Since, in a preferred
embodiment, the z-domain transfer function can be expressed as a fraction,
the numerator and denominator of the transfer function can be scaled so as
to allow the coefficients to be expressed as integers, thus making it possible
15 to calculate the filter coefficients from the aforementioned polynomial
interpolations using fixed-point math.

Brief Description of the Drawings

FIG. 1 is an exemplary perspective view of an exemplary disc drive;

FIG. 2 is an exemplary top plan view of the printed circuit board of
5 the exemplary disc drive of **Figure 1**;

FIG. 3 is a block diagram of a control system for a disc drive in
which the present invention may be utilized;

FIG. 4 is a flowchart representation of a process of deriving
interpolating polynomials for notch filter coefficients in accordance with a
10 preferred embodiment of the present invention; and

FIG. 5 is a flowchart representation of a process of deriving notch
filter coefficients using fixed-point math in accordance with a preferred
embodiment of the present invention.

Detailed Description

Referring now to the drawings, and initially to **FIG. 1**, there is
5 illustrated an example of a disc drive designated generally by reference
numeral **20**. Disc drive **20** includes a stack of storage discs **22a-d** and a
stack of read/write heads **24a-h**. Each of storage discs **22a-d** is provided
with a plurality of data tracks to store user data. As illustrated in **FIG. 1**,
one head is provided for each surface of each of storage discs **22a-d** such
10 that data can be read from or written to the data tracks of all of the storage
discs. The heads are coupled to pre-amplifier **31**. It should be understood
that disc drive **20** is merely representative of a disc drive system utilizing
the present invention and that the present invention can be implemented in
a disc drive system including more or less storage discs.

15 Storage discs **22a-d** are mounted for rotation by spindle motor
arrangement **29**, as is known in the art. Moreover, read/write heads **24a-h**
are supported by respective actuator arms **28a-h** for controlled positioning
over preselected radii of storage discs **22a-d** to enable the reading and
writing of data from and to the data tracks. To that end, actuator arms **28a-**
20 **h** are rotatably mounted on pin **30** by voice coil motor **32** operable to
controllably rotate actuator arms **28a-h** radially across the disc surfaces.

Each of read/write heads **24a-h** is mounted to a respective one of
actuator arm **28a-h** by a flexure element (not shown) and comprises a
magnetic transducer **25** mounted to slider **26** having an air bearing surface
25 (not shown), all in a known manner. As typically utilized in disc drive
systems, sliders **26** cause magnetic transducers **25** of the read/write heads
24a-h to "fly" above the surfaces of the respective storage discs **22a-d** for
non-contact operation of the disc drive system, as discussed above. When
not in use, voice coil motor **32** rotates actuator arms **28a-h** during a contact
30 stop operation, to position read/write heads **24a-h** over a respective one of

landing zones **58** or **60**, where read/write heads **24a-h** come to rest on the storage disc surfaces. As should be understood, each of read/write heads **24a-h** is at rest on a respective one of landing zones **58** or **60** at the commencement of a contact start operation.

5 Printed circuit board (PCB) **34** is provided to mount control electronics for controlled operation of spindle motor **29** and voice coil motor **32**. PCB **34** also includes read/write channel circuitry coupled to read/write heads **24a-h** via pre-amplifier **31**, to control the transfer of data to and from the data tracks of storage discs **22a-d**. The manner for coupling
10 PCB **34** to the various components of the disc drive is well known in the art, and includes connector **33** to couple the read/write channel circuitry to pre-amplifier **31**.

Referring now to **FIG. 2**, there is illustrated in schematic form PCB **34** and the electrical couplings between the control electronics on PCB **34**
15 and the components of the disc drive system described above. Microprocessor **35** is coupled to each of read/write control **36**, spindle motor control **38**, actuator control **40**, ROM **42** and RAM **43**. In modern disc drive designs, the microprocessor can comprise a digital signal processor (DSP). Microprocessor **35** sends data to and receives data from storage
20 discs **22a-d** via read/write control **36** and read/write heads **24a-h**.

Microprocessor **35** also operates according to instructions stored in ROM **42** to generate and transmit control signals to each of spindle motor control **38** and actuator control **40**.

Spindle motor control **38** is responsive to the control signals received
25 from microprocessor **35** to generate and transmit a drive voltage to spindle motor **29** to cause storage discs **22a-d** to rotate at an appropriate rotational velocity.

Similarly, actuator control **40** is responsive to the control signals received from microprocessor **35** to generate and transmit a voltage to
30 voice coil motor **32** to controllably rotate read/write heads **24a-h**, via

actuator arms **28a-h**, to preselected radial positions over storage discs **22a-d**. The magnitude and polarity of the voltage generated by actuator control **40**, as a function of the microprocessor control signals, determines the radial direction and radial speed of read/write heads **24a-h**.

5 When data to be written or read from one of storage discs **22a-d** are stored on a data track different from the current radial position of read/write heads **24a-h**, microprocessor **35** determines the current radial position of read/write heads **24a-h** and the radial position of the data track where read/write heads **24a-h** are to be relocated. Microprocessor **35** then
10 implements a seek operation wherein the control signals generated by microprocessor **35** for actuator control **40** cause voice coil motor **32** to move read/write heads **24a-h** from the current data track to a destination data track at the desired radial position.

 When the actuator has moved read/write heads **24a-h** to the
15 destination data track, a multiplexer (not shown) is used to couple read/write heads **24a-h** over the specific data track to be written or read, to read/write control **36**, as is generally known in the art. Read/write control **36** includes a read channel that, in accordance with modern disc drive design, comprises an electronic circuit that detects information represented
20 by magnetic transitions recorded on the disc surface within the radial extent of the selected data track. As described above, each data track is divided into a number of data sectors.

 During a read operation, electrical signals transduced by the head from the magnetic transitions of the data sectors are input to the read
25 channel of read/write control **36** for processing via pre-amplifier **31**. Random access memory (RAM) **43** can be used to buffer data read from or to be written to the data sectors of storage discs **22a-d** via read/write control **36**. The buffered data can be transferred to or from a host computer utilizing the disc drive for data storage.

The present invention is directed toward a method and apparatus for generating notch filter coefficients for a disc drive actuator arm control system using fixed-point arithmetic. FIG. 3 is a diagram of a disc drive actuator arm control system with which a preferred embodiment of the invention may be employed.

A digital command signal 300 for seeking or track-following is provided as input to summer 306, which combines command signal 300 with feedback from plant 304, which in a preferred embodiment is voice coil motor 32 in FIG. 1. In a preferred embodiment, this feedback from plant 304 will be the position error signal (PES) of a particular disc drive head. A digital controller 301 generates a signal from the output of summer 306 that minimizes plant disturbance and maintains tracking requirements. Notch filter 302 is interposed between summer 306 and plant 304 and is used to filter out resonant frequencies from the control signal sent to plant 304, so as to prevent the control system in FIG. 3 from becoming unstable. In a preferred embodiment notch filter 302 may actually comprise a cascade of multiple filters configured to filter out a number of different resonant frequencies.

A preferred embodiment of the present invention is implemented in the form of program code that is executed by a microprocessor within the disc drive. During the manufacturer's media certification process the resonant frequencies of the disc drive are ascertained by processes that are well-known to those skilled in the art. A preferred embodiment of the present invention uses these empirical resonant frequency measurements to derive coefficients for the actuator arm control system's notch filter. Although the calculations that are performed on the measured frequencies to obtain the coefficients are performed using fixed-point arithmetic, in order to best understand the principles of operation of a preferred embodiment of the present invention, it is helpful to delve into some mathematical analysis over the complex number system.

In analog signal processing, it is well-known and customary to express the transfer functions of system components as functions in the s -domain, i.e., as Laplace transforms. For example, the transfer function of a second-order notch filter is given as:

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$$T(s) = \frac{s^2 + (\frac{\omega_0}{Q_1}) + \omega_0^2}{s^2 + (\frac{\omega_0}{Q_2}) + \omega_0^2} \quad (1)$$

where ω_0 is the notch frequency (expressed in radians per second) and Q_1 and Q_2 are "quality factors," which are parameters that control the depth and width of the notch (stopband), respectively. The s -domain transfer
 10 function of a system is related to the frequency response of the system by the identity $s=j\omega$, where ω is a radian frequency and $j=\sqrt{-1}$.

Since the Laplace transform is a mathematical tool to performing analysis of continuous-time systems, the Laplace transform cannot be applied to digital (i.e., discrete-time) signal processing (at least not
 15 directly). Instead, the z -transform, which can be considered the discrete-time counterpart to the Laplace transform, is used. Since disc drives are generally digitally controlled, a preferred embodiment of the present invention uses fixed point arithmetic to calculate transfer function coefficients for a digital filter specified in terms of the discrete-time z -
 20 transform.

In practice, it is customary in the design of digital filters to first start with an s -domain transfer function for the desired filtering function and transform the s -domain transfer function in to a z -domain transfer function. One commonly employed transformation technique for transforming an s -
 25 domain transfer function into a z -domain transfer function is known as the bilinear transformation (also referred to as Tustin's rule). The concepts of the s -domain, z -domain, and bilinear transformation are well-known in the digital signal processing art, so there is no need to provide an elaborate and detailed discussion of these topics. Nonetheless, a brief description of how

the bilinear transformation is performed, as well as some of the notation used in describing digital and analog signal processing concepts, may be helpful to an understanding of a preferred embodiment of the present invention. The reader seeking a more detailed treatment of the topic is
 5 directed to Ashok Ambardar, *Analog and Digital Signal Processing*, PWS Publishing, 1995, or any of the many introductory textbooks in the field of digital signal processing.

A digital signal comprises a sequence of discrete values or samples, each representing a value of the signal at some point in time. A digital
 10 signal can be (and typically is) obtained from an analog signal by periodically sampling the magnitude of the analog signal over time to obtain the discrete digital signal values. The number of samples taken per second (i.e., the number of digital signal values representing a one-second interval of time) is referred to as the “sampling rate” of the digital signal,
 15 and is denoted as S_f . The sampling period $t_s = S_f^{-1}$ measures the amount of time between successive samples.

The concept of signal frequency is thus somewhat complicated for discrete-time signals, since there is both a sampling rate and whatever frequency components of the original sampled signal may exist. For
 20 example, a discrete-time representation of a sinusoidal function will have a signal frequency (i.e., the frequency of the sinusoid) as well as a sampling rate. The “digital frequency” Ω_D of a signal is given by $\Omega_D = \omega / t_s$, where ω is the radian signal frequency.

The bilinear transformation maps a function in the s-domain into the
 25 z-domain by performing the following substitution:

$$s \rightarrow \frac{2}{t_s} \left(\frac{z - 1}{z + 1} \right). \quad (2)$$

In practice, however, an enhanced form of the bilinear transformation, the bilinear transformation with prewarping, is used to reduce frequency-related distortion. Prewarping is used to match the

response of the z -domain function at digital frequency Ω_D to the response of the s -domain function at radian signal frequency ω . The bilinear transformation with prewarping utilizes the following substitution in place of that above:

$$s \rightarrow C \frac{z-1}{z+1}, \quad (3)$$

where C is defined as

$$C = \frac{\omega_A}{\tan(\frac{1}{2}\Omega_D)}. \quad (4)$$

The bilinear transformation, therefore, allows a transfer function in the z -domain to be derived from an s -domain transfer function. It is well known in the art that transfer functions in the z -domain are readily implemented in digital circuitry. Indeed, z -domain transfer functions provide the basis for digital filters and digital signal processing in general.

The present invention is concerned with the derivation of coefficients for z -domain transfer functions used for implementing digital notch filters in disc drives. Equation 1, above, provides the s -domain transfer function of a second-order notch filter. The bilinear transformation with prewarping can be used to transform this transfer function into a z -domain transfer function, as below:

$$T(z) = \frac{\left(C \frac{z-1}{z+1}\right)^2 + \frac{\omega_0}{Q_1} + \omega_0^2}{\left(C \frac{z-1}{z+1}\right)^2 + \frac{\omega_0}{Q_2} + \omega_0^2}. \quad (5)$$

Multiplying the numerator and denominator by $Q_1 Q_2 (z+1)^2$, multiplying out the parentheses, and collecting like terms yields

$$T(z) = \frac{a_2 z^2 + a_1 z + a_0}{b_2 z^2 + b_1 z + b_0}, \quad (6)$$

where

$$\begin{aligned}
a_2 &= Q_1 Q_2 C^2 + Q_2 \omega_0 + Q_1 Q_2 \omega_0^2, \\
a_1 &= 2Q_2 \omega_0 + 2Q_1 Q_2 \omega_0^2 - 2Q_1 Q_2 C^2, \\
a_0 &= Q_1 Q_2 C^2 + Q_1 Q_2 \omega_0^2 + Q_2 \omega_0, \\
b_2 &= Q_1 Q_2 C^2 + Q_1 \omega_0 + Q_1 Q_2 \omega_0^2, \\
b_1 &= 2Q_1 \omega_0 + 2Q_1 Q_2 \omega_0^2 - 2Q_1 Q_2 C^2, \\
b_0 &= Q_1 Q_2 C^2 + Q_1 Q_2 \omega_0^2 + Q_1 \omega_0.
\end{aligned}$$

Thus, for a particular filter design, $T(z)$ is the quotient of two polynomials in z . The particular frequency response of the filter, then, is determined by the values of the coefficients of these polynomials. Thus, a primary task of
5 a preferred embodiment of the present invention is to derive values for these coefficients using fixed-point math.

There are two primary challenges that a preferred embodiment of the present invention overcomes in order to compute these coefficients using fixed-point math. First, since Q , C , and ω_0 will generally have a
10 significant fractional component, it is necessary to use scaling in order to allow the polynomial coefficients to be expressed as integers without losing a great deal of accuracy. Since $T(z)$ is a fraction, Equation 6 can be scaled by simply multiplying the numerator and denominator by a constant K , where the choice of K will depend upon the general frequency range of
15 interest (*i.e.*, it is a design choice that can be made in advance).

The second challenge that a preferred embodiment of the present invention overcomes relates to the fact that in Equations 4 and 6, C is a nonlinear function of Ω_D , the digital frequency, since C contains the trigonometric tangent function. Computing a tangent function requires an
20 ability to compute fractions or decimals. Thus, it is not possible to apply Equation 6 directly using fixed-point math.

A preferred embodiment of the present invention, instead, uses polynomial interpolation to derive a value for each coefficient in Equation 6. There are a number of different techniques known in the art for deriving
25 a polynomial interpolation of a function. One particular technique that is well-known in the art is known as Lagrange polynomial interpolation. In

Lagrange polynomial interpolation, to approximate a function using an n th-degree polynomial, one first evaluates the original function, say $f(x)$, at $n+1$ points (x_0, x_1, \dots, x_n) in order to obtain a series of data points, $f(x_0), f(x_1), \dots, f(x_n)$. The n th-degree polynomial interpolation is given by

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$$p_n(x) = \sum_{i=0}^n l_i(x) f(x_i), \quad (7)$$

where the l_i 's are given by

$$l_i(x) = \prod_{j \neq i, j=0}^n \left(\frac{x - x_j}{x_i - x_j} \right). \quad (8)$$

10 One of ordinary skill in the art will recognize that the expressions given above for Lagrange polynomial interpolation can be expanded symbolically so that the expanded form of p_n can be determined by simply arithmetic evaluation in a computer. This, and other methods of polynomial interpolation, are well-known in the art as being readily
15 performed by a computer. The interested reader may consult any suitable undergraduate textbook in numerical analysis for further details regarding polynomial interpolation and other function-approximation techniques.

 In the context of a preferred embodiment of the present invention, a polynomial interpolation of each of each of the coefficient expressions in
20 the filter's transfer function is made. Specifically, each of the coefficient expressions in the transfer function is expressed as a function of the notch frequency ω_0 , and an interpolating polynomial in ω_0 is obtained.

 For example, consider the expression given in Equation 6 for the coefficient of z^2 in the numerator of the transfer function. We will then
25 treat this expression as a function f of the desired radian notch frequency ω , as below:

$$f(\omega) = Q_1 Q_2 C^2 + Q_2 \omega + Q_1 Q_2 \omega^2. \quad (9)$$

If we make the *a priori* design decisions to match the digital and analog transfer functions at the same radian notch frequency, use a sampling frequency of 13.32 kHz, and to use quality factors of $Q_1 = Q_2 = 1$, we can substitute Equation 4 into Equation 9 to obtain

$$f(\omega) = \left(\frac{\omega}{\tan(6660\omega)} \right)^2 + \omega + \omega^2. \quad (10)$$

Using floating-point math, we can evaluate $f(\omega)$ at $n+1$ points to obtain $f(\omega_0), f(\omega_1), \dots, f(\omega_n)$. In a preferred embodiment, $n=2$. To continue

with the example, let us suppose that we evaluate Equation 10 at

$\omega_0 = 2\pi \cdot 440$, $\omega_1 = 2\pi \cdot 880$, and $\omega_2 = 2\pi \cdot 1760$. We then obtain $f(\omega_0) \approx 7514402.33$, $f(\omega_1) \approx 30446290.00$, and $f(\omega_2) \approx 122168311.57$. Polynomial interpolation can then be performed on these values using either floating point math or by using fixed point math on rounded or truncated versions of the values. For example, Lagrange polynomial interpolation would proceed as below:

$$l_0(\omega) = \left(\frac{\omega - \omega_1}{\omega_0 - \omega_1} \right) \left(\frac{\omega - \omega_2}{\omega_0 - \omega_2} \right) = \left(\frac{\omega - 2\pi \cdot 880}{2\pi \cdot 440 - 2\pi \cdot 880} \right) \left(\frac{\omega - 2\pi \cdot 1760}{2\pi \cdot 440 - 2\pi \cdot 1760} \right) \quad (11)$$

$$l_1(\omega) = \left(\frac{\omega - \omega_0}{\omega_1 - \omega_0} \right) \left(\frac{\omega - \omega_2}{\omega_1 - \omega_2} \right) = \left(\frac{\omega - 2\pi \cdot 440}{2\pi \cdot 880 - 2\pi \cdot 440} \right) \left(\frac{\omega - 2\pi \cdot 1760}{2\pi \cdot 880 - 2\pi \cdot 1760} \right) \quad (12)$$

$$l_2(\omega) = \left(\frac{\omega - \omega_0}{\omega_2 - \omega_0} \right) \left(\frac{\omega - \omega_1}{\omega_2 - \omega_1} \right) = \left(\frac{\omega - 2\pi \cdot 440}{2\pi \cdot 1760 - 2\pi \cdot 440} \right) \left(\frac{\omega - 2\pi \cdot 880}{2\pi \cdot 1760 - 2\pi \cdot 880} \right) \quad (13)$$

$$p(\omega) = \sum_{i=0}^n l_i(\omega) f(\omega_i) \quad (14)$$

$$= l_0(\omega) f(\omega_0) + l_1(\omega) f(\omega_1) + l_2(\omega) f(\omega_2) \quad (15)$$

$$\approx \omega^2 + 30437996\omega - 84149059540. \quad (16)$$

Equation 16, above, shows that the interpolating polynomial $p(\omega)$ in our example can be evaluated using fixed-point math, since the only operations that are needed in order to evaluate $p(\omega)$ are addition,
5 subtraction and multiplication over the integers. Moreover, even if it is necessary to scale the z-domain transfer function from which $p(\omega)$ is derived (*i.e.*, by multiplying the numerator and denominator of the transfer function by a constant k), $p(\omega)$ can be easily scaled as well, simply by multiplying each term of $p(\omega)$ by k . Moreover, one of ordinary skill in the
10 art will recognize that a scaled form of ω , for example $\omega' = k \omega$ (k being the scale factor), may also be used by simply substituting ω' / k for ω in $p(\omega)$.

Thus, using the above-described techniques, each coefficient of a z-domain notch filter can be expressed as a polynomial over the integers that is a function of the desired radian notch frequency ω . Hence, appropriate
15 coefficients for a notch filter having a particular notch frequency may be calculated by a computer by supplying the notch frequency as input and evaluating the appropriate polynomial approximation for each coefficient in the z-domain transfer function of the filter. In a preferred embodiment, the interpolating polynomials for each coefficient are derived *a priori* using
20 floating-point math, and the disc drive is programmed to evaluate these polynomials using fixed-point math.

FIG. 4 is a flowchart representation of a process of deriving interpolating polynomials for use in calculating notch filter coefficients in accordance with a preferred embodiment of the present invention. The
25 bilinear transformation is used to take an s-domain transfer function and convert it into an equivalent z-domain transfer function (block 400). The z-domain transfer function so obtained is scaled so as to make the transfer function coefficients expressible as integers without significant loss of precision (block 402). Finally, polynomial interpolation is performed on
30 each of the expressions defining the coefficients in the z-domain transfer

function, so as to obtain interpolating polynomials that approximate the desired transfer function coefficients as functions of the filter's notch frequency (block 404).

FIG. 5 is a flowchart representation of a process of assigning
5 appropriate notch filter coefficients to a disc drive control system notch filter in accordance with a preferred embodiment of the present invention. A resonant frequency of the disc drive control system is first determined (block 500); in the case of several resonant frequencies, each is determined and the subsequent steps are performed with respect to each frequency, so
10 that a separate notch filter is derived for each notch frequency. Next, the approximating polynomials for each of the transfer function coefficients are evaluated at the resonant frequency (*i.e.*, the desired notch frequency for the filter) (block 502). Finally, the results of evaluating the approximating polynomials are used as the filter coefficients to program the digital notch
15 filter (block 504).

It is important to note that while the present invention has been described in the context of a fully functioning data processing system, those of ordinary skill in the art will appreciate that the processes of the present invention are capable of being distributed in the form of a
20 computer readable medium of instructions or other functional descriptive material and in a variety of other forms and that the present invention is equally applicable regardless of the particular type of signal bearing media actually used to carry out the distribution. Examples of computer readable media include recordable-type media, such as a floppy disk, a hard disk
25 drive, a RAM, CD-ROMs, DVD-ROMs, and transmission-type media, such as digital and analog communications links, wired or wireless communications links using transmission forms, such as, for example, radio frequency and light wave transmissions. The computer readable media may take the form of coded formats that are decoded for actual use
30 in a particular data processing system. Functional descriptive material is

information that imparts functionality to a machine. Functional descriptive material includes, but is not limited to, computer programs, instructions, rules, facts, definitions of computable functions, objects, and data structures.

5 The description of the present invention has been presented for purposes of illustration and description, and is not intended to be exhaustive or limited to the invention in the form disclosed. Many modifications and variations will be apparent to those of ordinary skill in the art. The embodiment was chosen and described in order to best
10 explain the principles of the invention, the practical application, and to enable others of ordinary skill in the art to understand the invention for various embodiments with various modifications as are suited to the particular use contemplated.